# GIROLAMO SACCHERI'S EUCLIDES VINDICATUS

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Girolamo Saccheri's Euclides vindicatus by George Bruce Halsted

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## GEORGE BRUCE HALSTED

# GIROLAMO SACCHERI'S EUCLIDES VINDICATUS



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# **EUCLIDES VINDICATUS**

EDITED AND TRANSLATED BY

GEORGE BRUCE HALSTED

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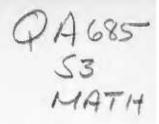
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### TABLE OF CONTENTS.

Translator's Preface         vii           Introduction         xv           Saccheri's Title-Page         3           Preface to the Reader         5           In Place of an Index         11           Proposition I.           Proposition III.         21           Proposition III.         21           Corollary I.         25           Corollary III.         27           Corollary III.         27           Proposition IV.         27           Definitions         29           Proposition V.         29           Proposition VII.         33           Proposition VIII.         37           Proposition VIII.         39           Proposition X.         41           Proposition X.         43           Proposition X.         45           Proposition	PAG	×
Saccheri's Title-Page       3         Preface to the Reader       5         In Place of an Index       11         Part I.         Proposition I.       21         Proposition III.       21         Corollary I.       25         Corollary III.       27         Corollary III.       27         Proposition IV.       27         Definitions       29         Proposition V.       29         Proposition VII.       37         Proposition VIII.       39         Proposition VIII.       39         Proposition XI.       41         Proposition XI.       45         Proposition XIII.       49         Proposition XIV.       50         Proposition XIV.       59         Proposition XVI.       61         Corollary       65         Proposition XVI.       67         Corollary       69         Proposition XVII.       69		
Preface to the Reader         5           In Place of an Index         11           PART I.           Proposition II.         21           Proposition III.         21           Corollary I.         25           Corollary III.         27           Corollary III.         27           Proposition IV.         27           Definitions         29           Proposition V.         29           Proposition VI.         33           Proposition VIII.         37           Proposition VIII.         39           Proposition XI.         41           Proposition XI.         45           Proposition XII.         49           Proposition XII.         53           Scholion I.         55           Scholion IV.         59           Proposition XV.         61           Corollary         65           Proposition XVI.         67           Corollary         69           Proposition XVII.	Introduction	v
Proposition I	Saccheri's Title-Page	3
Proposition I.	Preface to the Reader	5
Proposition II.       19         Proposition III.       21         Proposition III.       21         Corollary I.       25         Corollary III.       27         Corollary III.       27         Proposition IV.       27         Definitions       29         Proposition VI.       33         Proposition VII.       37         Proposition VIII.       39         Proposition IX.       41         Proposition XI.       45         Proposition XII.       49         Proposition XIII.       53         Scholion I.       55         Scholion II.       55         Proposition XIV.       59         Proposition XV.       61         Corollary       65         Proposition XVII.       67         Corollary       69         Proposition XVIII.       69         Proposition XVIII.       69          Proposition XVIII.       69		1
Proposition III.       21         Proposition III.       21         Corollary I.       25         Corollary III.       27         Proposition IV.       27         Definitions       29         Proposition V.       29         Proposition VII.       33         Proposition VIII.       39         Proposition IX.       41         Proposition X.       43         Proposition XII.       49         Proposition XIII.       53         Scholion I.       55         Scholion II.       55         Proposition XIV.       59         Proposition XV.       61         Corollary       65         Proposition XVI.       67         Corollary       69         Proposition XVII.       69         Proposition XVIII.       69          Proposition XVIII.       69		
Proposition III.       21         Corollary I.       25         Corollary III.       27         Corollary III.       27         Proposition IV.       27         Definitions       29         Proposition VI.       33         Proposition VII.       37         Proposition VIII.       39         Proposition IX.       41         Proposition X.       43         Proposition XII.       49         Proposition XIII.       53         Scholion I.       55         Scholion II.       55         Proposition XIV.       59         Proposition XV.       61         Corollary       65         Proposition XVI.       67         Corollary       69         Proposition XVII.       69         Proposition XVIII.       69          Proposition XVIII.       69		257
Corollary II.       25         Corollary III.       27         Corollary III.       27         Proposition IV.       27         Definitions       29         Proposition VI.       33         Proposition VIII.       37         Proposition VIII.       39         Proposition IX.       41         Proposition X.       43         Proposition XII.       49         Proposition XIII.       53         Scholion I.       55         Scholion II.       55         Proposition XIV.       59         Proposition XV.       61         Corollary       65         Proposition XVI.       67         Corollary       69         Proposition XVII.       69         Proposition XVII.       69		
Corollary III.       27         Corollary III.       27         Proposition IV.       27         Definitions       29         Proposition V.       29         Proposition VII.       33         Proposition VIII.       39         Proposition IX.       41         Proposition X.       43         Proposition XII.       49         Proposition XIII.       53         Scholion I.       55         Scholion II.       55         Proposition XIV.       59         Proposition XV.       61         Corollary       65         Proposition XVII.       67         Corollary       69         Proposition XVIII.       69		
Corollary III.       27         Corollary III.       27         Proposition IV.       27         Definitions       29         Proposition V.       29         Proposition VII.       33         Proposition VIII.       39         Proposition IX.       41         Proposition X.       43         Proposition XII.       49         Proposition XIII.       53         Scholion I.       55         Scholion II.       55         Proposition XIV.       59         Proposition XV.       61         Corollary       65         Proposition XVII.       67         Corollary       69         Proposition XVIII.       69	Corollary I	5
Corollary III.       27         Proposition IV.       27         Definitions       29         Proposition V.       29         Proposition VII.       33         Proposition VIII.       39         Proposition IX.       41         Proposition X.       43         Proposition XII.       49         Proposition XIII.       53         Scholion I.       55         Scholion II.       55         Proposition XIV.       59         Proposition XV.       61         Corollary       65         Proposition XVII.       67         Corollary       69         Proposition XVIII.       69         Proposition XVIII.       69		
Proposition IV.         27           Definitions         29           Proposition V.         29           Proposition VII.         33           Proposition VIII.         39           Proposition IX.         41           Proposition X.         43           Proposition XII.         49           Proposition XIII.         53           Scholion I.         55           Scholion II.         55           Proposition XIV.         59           Proposition XV.         61           Corollary         65           Proposition XVII.         67           Corollary         69           Proposition XVIII.         69           Proposition XVIII.         69		
Definitions         29           Proposition V.         29           Proposition VI.         33           Proposition VIII.         37           Proposition VIII.         39           Proposition IX.         41           Proposition X.         43           Proposition XII.         49           Proposition XIII.         53           Scholion I.         55           Scholion II.         55           Proposition XIV.         59           Corollary         65           Proposition XVI.         67           Corollary         69           Proposition XVII.         69           Proposition XVII.         69           Proposition XVIII.         69		
Proposition V.         29           Proposition VI.         33           Proposition VIII.         37           Proposition VIII.         39           Proposition IX.         41           Proposition X.I.         45           Proposition XII.         49           Proposition XIII.         53           Scholion I.         55           Scholion II.         55           Proposition XIV.         59           Corollary         65           Proposition XVI.         67           Corollary         69           Proposition XVII.         69           Proposition XVII.         69           Proposition XVIII.         69		
Proposition VI.         33           Proposition VII.         37           Proposition VIII.         39           Proposition IX.         41           Proposition X.I.         45           Proposition XII.         49           Proposition XIII.         53           Scholion I.         55           Scholion II.         55           Proposition XIV.         59           Corollary         65           Proposition XVI.         67           Corollary         69           Proposition XVII.         69           Proposition XVIII.         69		
Proposition VII.         37           Proposition VIII.         39           Proposition IX.         41           Proposition X.         43           Proposition XII.         45           Proposition XIII.         53           Scholion I.         55           Scholion II.         55           Proposition XIV.         59           Corollary         65           Proposition XVI.         67           Corollary         69           Proposition XVII.         69           Proposition XVII.         69	Proposition VI	13
Proposition VIII.         39           Proposition IX.         41           Proposition X.         43           Proposition XII.         45           Proposition XIII.         53           Scholion I.         55           Scholion II.         55           Proposition XIV.         59           Proposition XV.         61           Corollary         65           Proposition XVI.         67           Corollary         69           Proposition XVII.         69           Proposition XVIII.         69	Proposition VII	17
Proposition IX.         41           Proposition X.         43           Proposition XI.         45           Proposition XIII.         49           Proposition XIII.         53           Scholion I.         55           Scholion II.         55           Proposition XIV.         59           Proposition XV.         61           Corollary         65           Proposition XVI.         67           Corollary         69           Proposition XVII.         69		19
Proposition XI         45           Proposition XIII.         49           Proposition XIII.         53           Scholion I.         55           Scholion III.         55           Proposition XIV.         59           Proposition XV.         61           Corollary.         65           Proposition XVI.         67           Corollary.         69           Proposition XVII.         69           Proposition XVII.         69		11
Proposition XI.         45           Proposition XII.         49           Proposition XIII.         53           Scholion I.         55           Scholion II.         55           Proposition XIV.         59           Proposition XV.         61           Corollary         65           Proposition XVI.         67           Corollary         69           Proposition XVII.         69	Proposition X	13
Proposition XII.         49           Proposition XIII.         53           Scholion I.         55           Scholion II.         55           Proposition XIV.         59           Proposition XV.         61           Corollary         65           Proposition XVI.         67           Corollary         69           Proposition XVII.         69	Proposition XI	15
Proposition XIII.         53           Scholion I.         55           Scholion II.         55           Proposition XIV.         59           Proposition XV.         61           Corollary         65           Proposition XVI.         67           Corollary         69           Proposition XVII.         69	Proposition XII.	19
Scholion I.         55           Scholion II.         55           Proposition XIV.         59           Proposition XV.         61           Corollary.         65           Proposition XVI.         67           Corollary.         69           Proposition XVII.         69		3
Scholion II.         55           Proposition XIV.         59           Proposition XV.         61           Corollary.         65           Proposition XVI.         67           Corollary.         69           Proposition XVII.         69	100 To 10	55
Proposition XIV.         59           Proposition XV.         61           Corollary.         65           Proposition XVI.         67           Corollary.         69           Proposition XVII.         69		55
Proposition XV.         61           Corollary.         65           Proposition XVI.         67           Corollary.         69           Proposition XVII.         69		99
Corollary         65           Proposition XVI         67           Corollary         69           Proposition XVII         69	Proposition XV.	51
Proposition XVI.         67           Corollary         69           Proposition XVII.         69	Corollary	55
Corollary	Proposition XVI	7
Proposition XVII	Corollary	şç
The state of the s		
	The state of the s	
Scholion II		13

AND AND SERVICES	PAGE
Proposition XVIII	
Proposition XIX	
Proposition XX	
Proposition XXI	81
Corollary	
Scholion I	83
Scholion II	87
Scholion III	101
Scholion IV	109
Proposition XXII	113
Proposition XXIII	
Corollary I	
Scholion	121
Corollary II	
Proposition XXIV	125
Corollary	127
Scholion	
Proposition XXV	131
Corollary I	137
Corollary II	137
Proposition XXVI	
Corollary I	141
Corollary II.	141
Corollary III	143
Proposition XXVII	
Scholion I	147
Scholion II	149
Scholion III.	149
Proposition XXVIII	149
Corollary	157
Proposition XXIX	157
Corollary I	159
Corollary II	159
Proposition XXX,	161
Corollary	165
Proposition XXXI	167
Proposition XXXII	
Proposition XXXIII	173
Lemma I	173
Corollary I	177
Corollary II	179
Lemma II	179
Corollary	195
Lemma III.	197
Lemma IV.	199

	PAGE
Scholion	201
Lemma V	201
Corollary	370.77
Scholion	
Scholon	201
PART II.	
Proposition XXXIV	209
Proposition XXXV.	211
Proposition XXXVI	213
Corollary	215
Proposition XXXVII	215
Scholion I	221
Scholion II,	225
Proposition XXXVIII	225
Scholion	
Proposition XXXIX.	231
Scholion	
Notes	243
Translator's Subject Index	245
Translator's Index of Proper Names	

### TRANSLATOR'S PREFACE.

Saccheri was discovered accidentally by Father Manganotti, S. J., in 1889, a discovery which could not have happened on the Western Continent, as it was only my instant realization of the treasure found which then, through my friend Prof. Paul Mansion, drew to me overseas the first Saccheri ever to have crossed the ocean. This, upon my securing Earl Stanhope's copy, I sent back, to be whelmed in a common death with the dearly beloved Mansion and the magnificent Alberto Pascal.

How rare, practically extinct, Saccheri has been is illustrated by the fact that the greatest of living non-Euclideans, Prof. Paul Barbarin, though resident in the world's capital, Paris, the modern Alexandria, yet sent, as I had done before him, to Mansion for a glimpse of this pearl of great price; and again by the fact that no one has remarked that the erudite and accurate Sir Thomas Heath, in his three-volumed masterpiece, has listed Saccheri's Euclides vindicatus as a Latin edition of Euclid, calling Saccheri its editor, a mistake so gross it could never have been made by any one who had been privileged to see Saccheri's diadem.

Does it not seem to be the irony of fate that the only existing copy of the posthumous edition of Saccheri's won-derful Logica demonstrativa reposes in the "Stadtbibliothek" of the foreign city built by Nero's mother—Colonia Agrippina on the banks of the Rhine? May the present volume help to avert from it the imminent peril of perishing for-