

**PROBLEMS IN DIFFERENTIAL  
CALCULUS: SUPPLEMENTARY  
TO A TREATISE ON  
DIFFERENTIAL CALCULUS**

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Problems in Differential Calculus: Supplementary to a Treatise on differential calculus by W. E. Byerly

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**W. E. BYERLY**

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PROBLEMS  
IN  
DIFFERENTIAL CALCULUS

SUPPLEMENTARY TO A TREATISE ON  
DIFFERENTIAL CALCULUS

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## PREFACE.

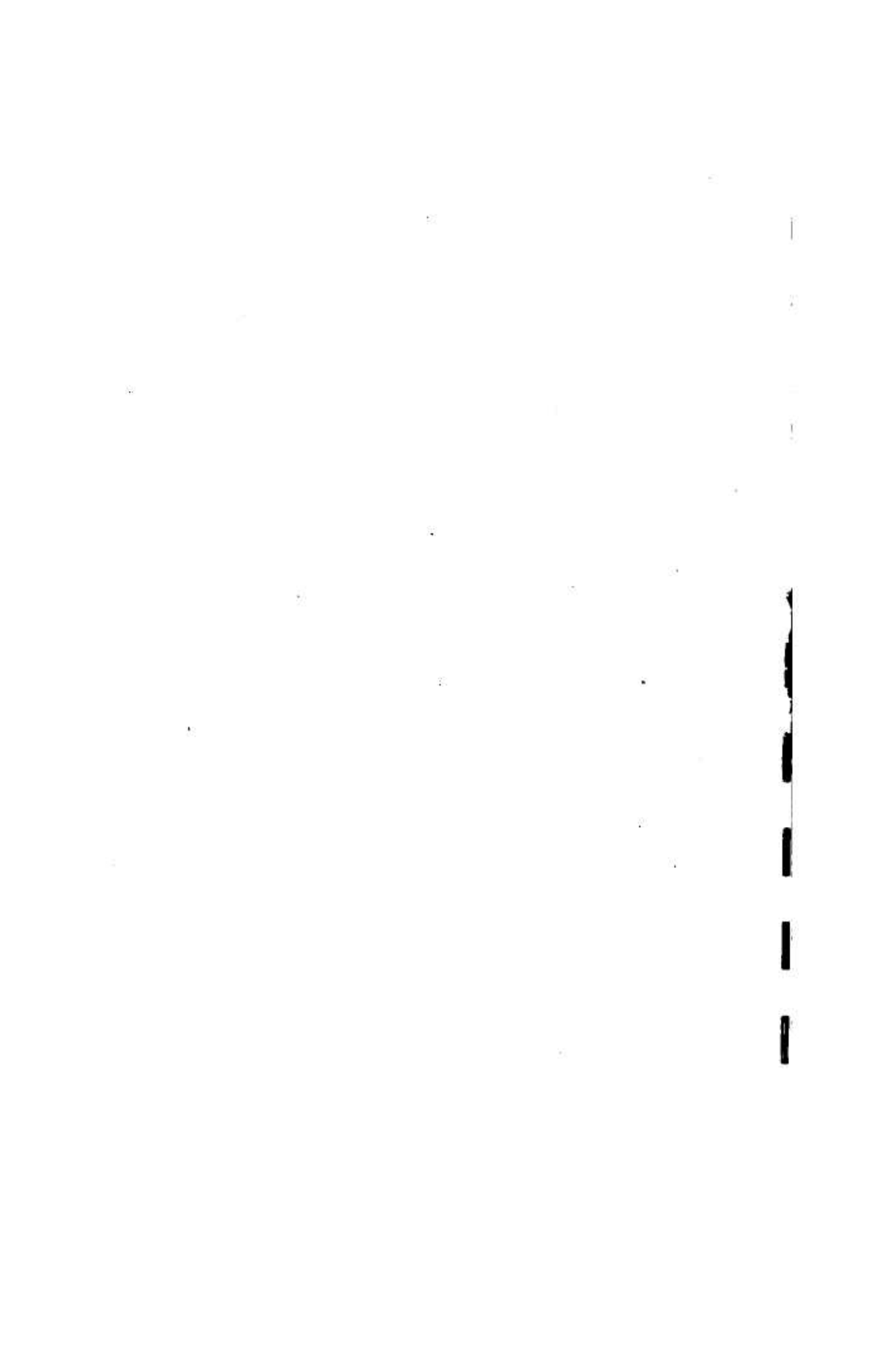
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THIS collection of problems and examples is intended to accompany and to supplement my treatise on the Differential Calculus (Boston, Ginn & Company). The chapters correspond to the chapters in that book and the references are to its sections.

A slightly fuller treatment of definite integrals and of development in series than that in the original text is indicated and illustrated, and brief explanations and suggestions are given when they seem to me to be needed.

W. E. BYERLY.

CAMBRIDGE, MASS.,  
Sept. 20, 1895.





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