

**THE ELEMENTARY  
PRINCIPLES OF  
MECHANICS.  
VOL. I. KINEMATICS**

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The Elementary Principles of Mechanics. Vol. I. Kinematics by A. Jay Du Bois

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**A. JAY DU BOIS**

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ELEMENTARY PRINCIPLES  
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MECHANICS.

VOL. I  
KINEMATICS.

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NOTE.

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The large type by itself constitutes an abridged course.  
Articles in small type are for advanced students.  
Articles containing applications of the Calculus are enclosed  
in brackets.

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