

**OLNEY'S MATHEMATICAL
SERIES. ELEMENTS
OF TRIGONOMETRY:
PLANE AND SPHERICAL**

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EDWARD OLNEY

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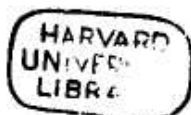
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