

**AN ELEMENTARY TREATISE ON PLANE  
TRIGONOMETRY; WITH A NUMEROUS  
COLLECTION OF EXAMPLES, CHIEFLY  
DESIGNED FOR THE USE OF SCHOOLS  
AND BEGINNERS**

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An Elementary Treatise on Plane Trigonometry; With a Numerous Collection of Examples,  
Chiefly Designed for the Use of Schools and Beginners by R. D. Beasley

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**R. D. BEASLEY**

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## PLANE TRIGONOMETRY.

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ON  
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WITH  
A Numerous Collection of Examples,

CHIEFLY DESIGNED FOR THE USE OF SCHOOLS AND BEGINNERS.

BY  
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## PREFACE.

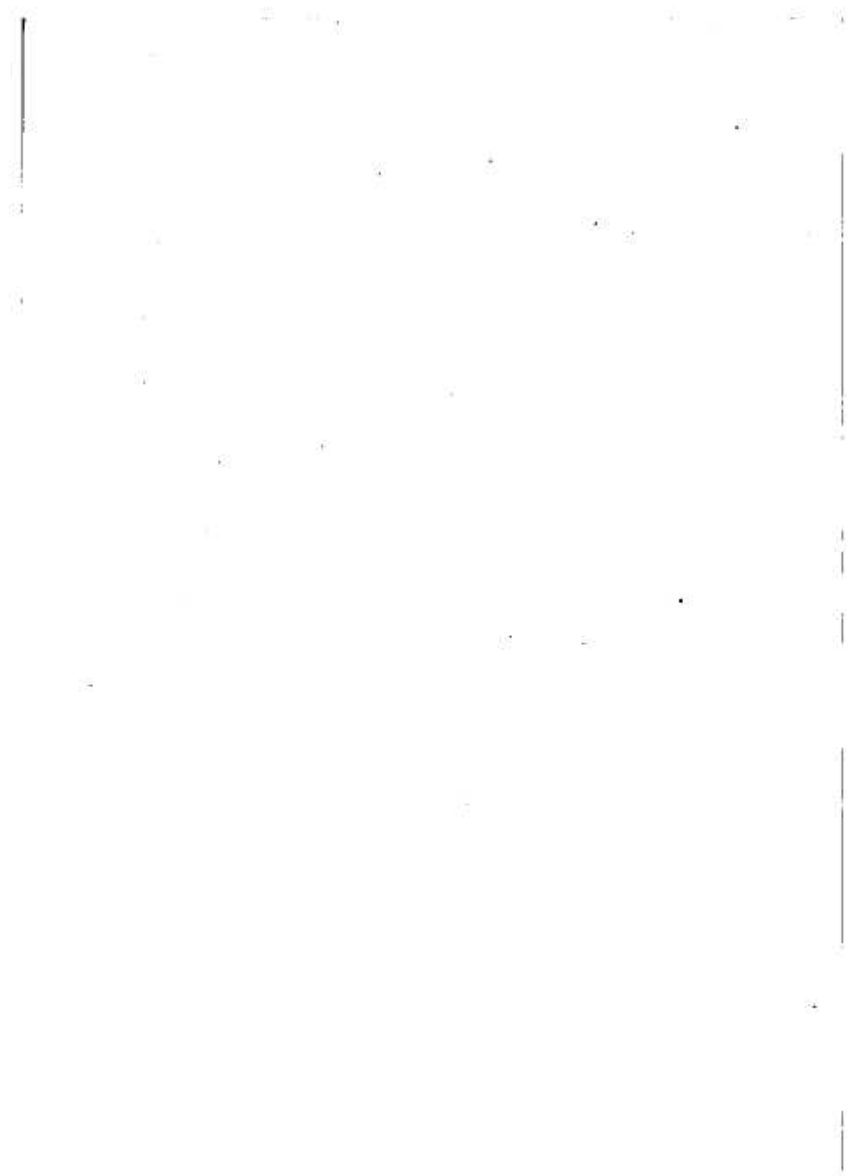
THE following pages are specially intended for use in Schools. In the choice of matter I have been chiefly guided by the requirements of the three days' Examination at Cambridge, with the exception of proportional parts in logarithms, which I have omitted. In one point, I have ventured to deviate from the usual custom. I have denoted angles throughout by the Greek characters, even before the explanation of circular measure. My reasons for doing so were chiefly two; first, that they are much more distinctly and easily written, and it is advisable that a boy should be accustomed in the text to the notation he uses on his paper; secondly, I am thus enabled to insert the algebraical symbols for the angles in the figures, a very great advantage in such propositions as that proved in Art. 27. I have added about 400 examples mainly collected from the Examination Papers of the last ten years, and I have taken great pains to exclude from the body of the work any which might dishearten a beginner by their difficulty.

In conclusion, I must express my great obligations to my friend the Rev. R. B. Mayor, of Rugby. Without his kind encouragement I should not have ventured to have offered these pages to the public; and I am indebted to him, not only for many valuable suggestions, but for a careful revision of the whole work.

R. D. BEASLEY.

ST JOHN'S COLLEGE, CAMBRIDGE,  
*September, 1858.*





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