

**DIFFERENTIAL AND  
INTEGRAL CALCULUS  
FOR TECHNICAL  
SCHOOLS AND COLLEGES**

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Differential and Integral Calculus for Technical Schools and Colleges by P. A. Lambert

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**P. A. LAMBERT**

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FOR TECHNICAL  
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**DIFFERENTIAL AND INTEGRAL  
CALCULUS**

The  Co.

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DIFFERENTIAL AND INTEGRAL  
CALCULUS

FOR  
*TECHNICAL SCHOOLS AND COLLEGES*

BY  
P. A. LAMBERT, M.A.  
ASSISTANT PROFESSOR OF MATHEMATICS, LEHIGH UNIVERSITY

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## PREFACE

THIS text-book on the Differential and Integral Calculus is intended for students who have a working knowledge of Elementary Geometry, Algebra, Trigonometry, and Analytic Geometry.

The object of the text-book is threefold :

By a logical presentation of principles to inspire confidence in the methods of infinitesimal analysis.

By numerous problems to aid in acquiring facility in applying these methods.

By applications to problems in Physics and Engineering, and other branches of Mathematics, to show the practical value of the Calculus.

The division of the subject-matter according to classes of functions, makes it possible to introduce these applications from the start, and thereby arouse the interest of the student.

The simultaneous treatment of differentiation and integration, and the use of trigonometric substitution to simplify integration, economize the time and effort of the student.

P. A. LAMBERT.

Year	Number of cases		Rate per 100,000
	Male	Female	
1980	10	10	10
1981	10	10	10
1982	10	10	10
1983	10	10	10
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2028	10	10	10
2029	10	10	10
2030	10	10	10

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