

**ELEMENTS OF DYNAMIC: AN
INTRODUCTION TO THE STUDY
OF MOTION AND REST IN SOLID
AND FLUID BODIES. PART I.
KINEMATIC**

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W. K. CLIFFORD

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AN INTRODUCTION TO THE STUDY OF

MOTION AND REST

IN SOLID AND FLUID BODIES

BY

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