

# **KEY TO PLANE GEOMETRY**

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Key to Plane Geometry by Fletcher Durell & E. E. Arnold

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**FLETCHER DURELL & E. E. ARNOLD**

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GEOMETRY**



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TO  
PLANE GEOMETRY

BY

FLETCHER DURELL, Ph.D.

HEAD OF THE MATHEMATICAL DEPARTMENT IN THE  
LAWRENCEVILLE SCHOOL

AND

E. E. ARNOLD

SPECIALIST IN MATHEMATICS IN THE UNIVERSITY OF  
THE STATE OF NEW YORK



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## PAGE 20

24.  $x = 2(90^\circ - x)$ .  $\therefore x = 60^\circ$ . *Ans.*  
 25.  $x = \frac{1}{2}(180^\circ - x)$ .  $\therefore x = 45^\circ$ . *Ans.*  
 26.  $x = \frac{1}{3}(180^\circ - x)$ .  $\therefore x = 80^\circ$ . *Ans.*  
 27. (1)  $x = 90^\circ - x + 12^\circ$ .  $\therefore x = 51^\circ$ . *Ans.*  
 (2)  $x = 180^\circ - x + 15\frac{1}{2}^\circ$ .  $\therefore x = 97^\circ 45'$ . *Ans.*  
 28.  $90^\circ - x + 180^\circ - x = 126^\circ$ .  $\therefore x = 72^\circ$ . *Ans.*  
 29.  $180^\circ - x = 4(90^\circ - x)$ .  $\therefore x = 60^\circ$ . *Ans.*

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2. Yes, by placing the edge of the ruler on the pipe in a direction parallel to the length of the pipe. No.  
 3. No.  
 4. Place the straight edge on the surface in various directions. In all positions every point of the straight edge should be in contact with the surface of the tennis court.  
 5. Yes.

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1. Ax. 7. 2.  $140^\circ$ ;  $210^\circ$ ; Ax. 7.  
 3. 
$$\begin{array}{r} 7 = 7 \\ - 2 = - 2 \\ \hline 5 = 5 \end{array}$$
  
 4. (1) 
$$\begin{array}{r} 5 = 5 \\ \times 2 \quad \times 2 \\ \hline 10 = 10 \end{array}$$
  
 (2)  $12 = 12$ . Dividing each of these by 3,  $4 = 4$ .  
 5.  $8 = 8$ .  $\therefore \sqrt[3]{8} = \sqrt[3]{8}$ , or  $2 = 2$ .  
 6. Ax. 4.

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7. Ax. 2.  
 8. Use the diagram of Ex. 7. Thus, if  $LN = MO$ , then  $LM = NO$  (Ax. 3).  
 11. Ax. 1. 12. Ax. 2. 13. Ax. 9.  
 14. Through two points only one straight line can be passed; and a right angle is half of a straight angle.







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6.  $y = m$  (§ 82).  $x = y$  (§ 97);  $l = m$  (§ 97), etc.
7. Prove  $\triangle ABD = \triangle BFC$  by § 79, etc.
8.  $\angle B = \angle C$  (§ 82). Then use § 96 twice and Ax. 1.
9.  $\angle CBE = 115^\circ$  (Ax. 7).  $\therefore \angle ABE = 65^\circ$  (§ 32).  
 $\therefore BE \parallel CD$  (§ 91).
10.  $\angle B = \angle i$  (step 6, p. 43), etc.

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- |                     |                 |        |
|---------------------|-----------------|--------|
| 1. $62^\circ$ .     | 3. $60^\circ$ . | 5. No. |
| 2. $53^\circ 45'$ . | 4. $45^\circ$ . |        |

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- |  |                 |  |
|--|-----------------|--|
| 6. $138^\circ$ .                             | 8. $71^\circ$ . | 10. $78^\circ$ ; $78^\circ$ ; $24^\circ$ . |
| 7. $142^\circ$ ; $115^\circ$ ; $103^\circ$ . | 9. $80^\circ$ . |  |
11. Construct an equilateral triangle and bisect one of its angles. Bisect an angle of  $30^\circ$ .
  12. Construct the supplement of  $60^\circ$ .  $75^\circ = 45^\circ + 30^\circ$ .
  13.  $150^\circ = 90^\circ + 60^\circ$ .  $195^\circ = 180^\circ + 15^\circ$ .
  15. Construct an equilateral triangle and a perpendicular to the base through an extremity of the base.
  16. See Ex. 12.
  17. Construct an angle of  $45^\circ$  at each end of the 2-in. line.
  19. Corr.  $\sphericalangle$  are = (§ 107).  $\triangle$  are not equal.
  20. Through the vertex of the acute angle construct a  $\perp$  to one side of the angle.
  21. Produce one side of the angle through the vertex.

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- |               |                        |
|---------------|------------------------|
| 1. Use § 114. | 3. $\angle B$ (§ 114). |
| 2. § 114.     | 4. § 114.              |
5.  $\angle OAQ = \angle OBP$  (§ 114).  
 $\angle AOQ = \angle BOP$  (§ 69).  
 $\angle AOB = \angle POQ$  (§ 69).  
 $\angle AQB = \angle OQC = \angle APC = \angle APB$  (§ 63).
  6. See Ex. 1, p. 39.