

**FIRST-YEAR
MATHEMATICS FOR
SECONDARY SCHOOLS**

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First-year Mathematics for Secondary Schools by George William Myers

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GEORGE WILLIAM MYERS

**FIRST-YEAR
MATHEMATICS FOR
SECONDARY SCHOOLS**

First-Year Mathematics

For Secondary Schools

By

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