

ANALYTIC GEOMETRY

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Analytic Geometry by H. B. Phillips

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H. B. PHILLIPS

**ANALYTIC
GEOMETRY**

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BY

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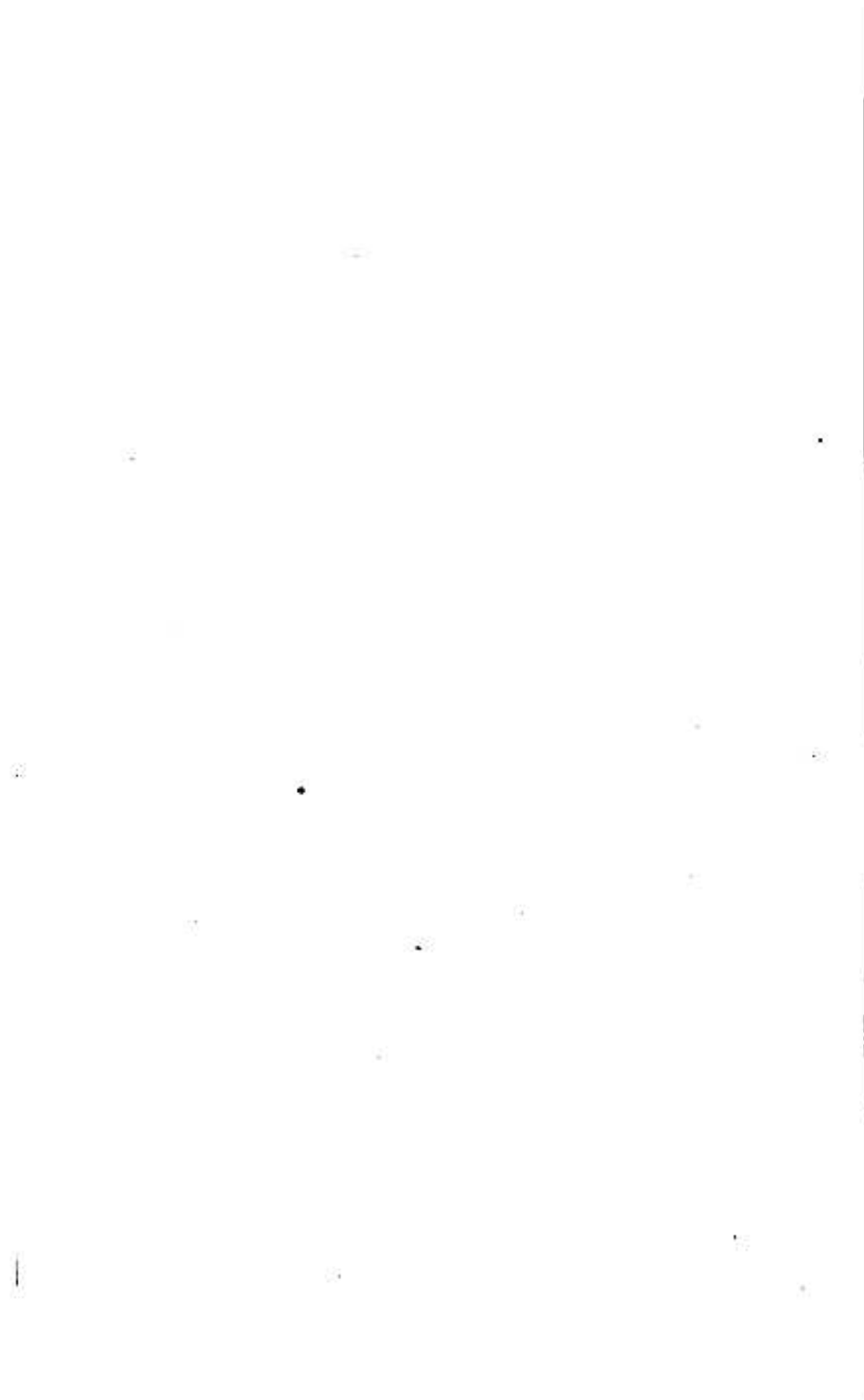
PREFACE

THE author of this text believes that the differential calculus should be given to the student in college at the earliest possible moment, and that to accomplish this a short course in analytic geometry is essential. He has, therefore, written this text to supply a course that will equip the student for work in calculus and engineering without burdening him with a mass of detail useful only to the student of mathematics for its own sake. The exercises are so numerous and varied that the teacher who desires to spend a longer time on analytic geometry can easily do so; and, indeed, if more than the briefest course is given, the best way to spend the time is in working a large number of varied examples based upon the few fundamental principles which occur constantly in practice.

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H. B. PHILLIPS

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CONTENTS

CHAPTER 1

ALGEBRAIC PRINCIPLES

NO.		PAGE
1.	Constants and variables ✓	1
2.	Equations	3
3.	Equations in one variable	5
4.	Factors and roots	7
5.	Approximate solution of equations	9
6.	Inequalities ✓	11
7.	Simultaneous equations	12
8.	Special cases	14
9.	Undetermined coefficients	16
10.	Functions ✓	18

CHAPTER 2

RECTANGULAR COÖRDINATES

11.	Definitions ✓	23
12.	Segments	26
13.	Projection	27
14.	Distance between two points	29
15.	Vectors ✓	32
16.	Multiple of a vector	35
17.	Addition and subtraction of vectors	36
18.	Slope of a line	39
19.	Graphs	43
20.	Equation of a locus	47
21.	Point on a locus	49
22.	Tangent curves	51

CHAPTER 3

STRAIGHT LINE AND CIRCLE

23.	Equation of a straight line	54
24.	First degree equation	57
25.	The expression $Ax + By + C$	60

Num.	PAGE
26. Distance from a point to a line	61
27. Equation of a circle	64
28. Circle determined by three conditions	66

CHAPTER 4

SECOND DEGREE EQUATIONS

29. The ellipse	70
30. The ellipse in other positions	71
31. The parabola	74
32. The hyperbola	77
33. The rectangular hyperbola	80
34. The second degree equation	83
35. Locus problems	87

CHAPTER 5

GRAPHS AND EMPIRICAL EQUATIONS

36. Intersections with the coördinate axes	90
37. Real and imaginary coördinates	92
38. Symmetry	93
39. Infinite values	95
40. Direction of the curve	96
41. Sine curves	99
42. Periodic functions	102
43. Exponential and logarithmic curves	104
44. Empirical equations	107

CHAPTER 6

POLAR COÖRDINATES

45. Definitions	113
46. Change of coördinates	116
47. Straight line and circle	117
48. The conic	117
49. Graphing equations	121
50. Intersections of curves	124
51. Locus problems	127

CHAPTER 7

PARAMETRIC REPRESENTATION

52. Definition of parameter	130
53. Locus of parametric equations	132
54. Parametric from coördinate equations	135
55. Locus problems	138

CONTENTS

vii

CHAPTER 8

TRANSFORMATION OF COÖRDINATES

ART.	PAGE
56. Translation of the axes	142
57. Rotation of the axes	144
58. Invariants	145
59. General equation of the second degree	146

CHAPTER 9

COÖRDINATES OF A POINT IN SPACE

60. Rectangular coördinates	150
61. Projection	151
62. Distance between two points	154
63. Vectors	155
64. Direction of a line	156
65. The angle between two directed lines	158
66. Cylindrical and spherical coördinates	160

CHAPTER 10

SURFACES

67. Loci	163
68. Equation of a plane	163
69. Equation of a sphere	167
70. Equation of a cylindrical surface	167
71. Surface of revolution	168
72. Graph of an equation	170

CHAPTER 11

LINES AND CURVES

73. The straight line	176
74. Curves	178
75. Parametric equations	180