

**A TREATISE ON THE
THEORY OF ALGEBRAICAL
EQUATIONS**

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A Treatise on the Theory of Algebraical Equations by J. Hymers

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Figure 1. Scatter plot showing the relationship between the number of children and the number of books. The solid line represents a strong positive correlation, while the dashed line represents a weaker correlation.

TREATISE

ON

ALGEBRAICAL EQUATIONS.



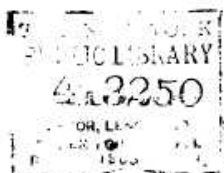
A TREATISE
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OF
ALGEBRAICAL EQUATIONS.

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