

**UNITED STATES COAST
AND GEODETIC
SURVEY. A TREATISE ON
PROJECTIONS, PP. 1-243**

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THOMAS CRAIG

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AND GEODETIC
SURVEY. A TREATISE ON
PROJECTIONS, PP. 1-243**

Alexander Leitch

UNITED STATES
COAST AND GEODETIC SURVEY

CARLILE P. PATTERSON
SUPERINTENDENT

A TREATISE

ON

PROJECTIONS

BY

THOMAS CRAIG



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1878. }

PART I.

MATHEMATICAL THEORY OF PROJECTIONS.

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PART I.

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