A TREATISE ON PROBABILITY: FORMING THE ARTICLE UNDER THAT HEAD IN THE SEVENTH EDITION OF THE ENCYCLOPAEDIA BRITANNICA

Published @ 2017 Trieste Publishing Pty Ltd

ISBN 9780649068067

A Treatise on Probability: Forming the Article Under that Head in the Seventh Edition of the Encyclopaedia Britannica by Thomas Galloway

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THOMAS GALLOWAY

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BY

THOMAS GALLOWAY, M.A. F.R.S.

SECRETARY OF THE ROYAL ASTRONOMICAL SOCIETY.

EDINBURGH:

ADAM AND CHARLES BLACK, NORTH BRIDGE,

BOOKSELLERS TO HER MAJESTY FOR SCOTLAND.

1839.

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Hamilton
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The Reader is requested to substitute the following List of Errata for that at the end of the volume.

ERRATA.

Page 40, *note*, for *Essai sur les Probabilités*, read *Théorie Analytique des Probabilités*.

— 43, line 7 from foot, for *adopt* read *adopt*.

— 49, line 13, read beginning *with*. In the note, read *Traité Elémentaire*.

— 54, line 7, for $a-m$, read $a-m'$.

— 81, first line, for $(1+2+3...+)n$, read $(1+2+3...+n)$.

— 89, line 9, for $m-m$, read $m+m'$.

— 135, last line, for $(n+x)^{-n+x-1}$, read $(n+x)^{-n-x-1}$.

— 188 line 8, for e^{-z}, read $e^{-\beta^2}$.

— 193, line 8, delete *products of the*.

— 198, line 9, for e', e'', read $e'e''$.

— 203, line 19, for *kc'*, read *kc*.

— — line 3 from foot, for (1), read (2).

— 209, last line, for *les* read *des*.

— 210, line 2 from foot, for 1833, 1834, *and* 1835, read 1834, 1835, *and* 1836.

— 211, last line, for *Abhandlungen*, read *Nachrichten*.